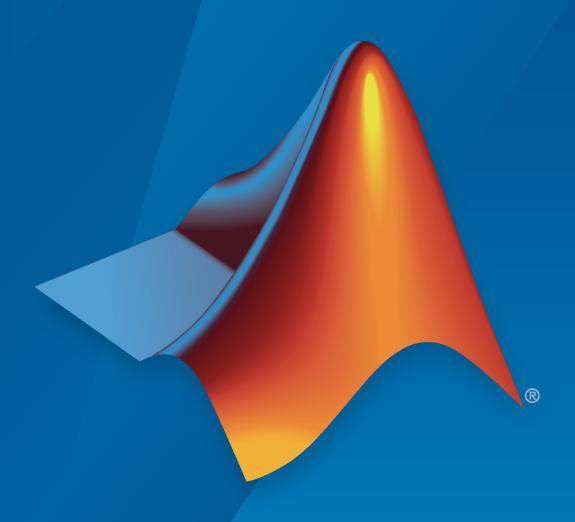# Partial Differential Equation Toolbox™ Release Notes

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Contents

R2015b

R2015a

R2021b

Version: 3.7

New Features

Bug Fixes

Electromagnetic Analysis: Solve 3-D electrostatic and magnetostatic problems

The programmatic workflow for electromagnetic analysis enables you to set up, solve, and analyze 3-D electrostatic and magnetostatic problems using natural steps and familiar domain-specific language.

For more details about the new workflow, see "Electromagnetics".

Local Mesh Refinement: Set target mesh sizes around specified vertices, edges, and faces

The `generateMesh` function lets you specify local target mesh size around geometric vertices, edges, and faces. The function generates a mesh with the element sizes around the specified regions as close to the target sizes as possible, and gradually blends the mesh between regions with different element sizes.

Structural and Thermal Analysis: Extract sparse linear models for use with Control System Toolbox

Use the `linearize` function to obtain `mechss` and `sparss` models from structural and thermal models, respectively. You can also use the function to extract the finite element matrices used to obtain the `mechss` and `sparss` models. For examples, see "Linear Analysis of Cantilever Beam" (Control System Toolbox) and "Linear Analysis of Tuning Fork" (Control System Toolbox).

PDEVisualization Properties: Display or hide axes and control background color

Use PDEVisualization Properties to display or hide the axes and also change the background color.

R2021a

Version: 3.6

New Features

Bug Fixes

Electromagnetic Analysis: Solve 2-D electrostatic and magnetostatic problems

A new programmatic workflow lets you set up, solve, and analyze 2-D electrostatic and magnetostatic problems using natural steps and familiar domain-specific language. When setting up an electromagnetic problem, you can:

- Create a special model container for an electrostatic or magnetostatic model using the `createpde` function.
- Assign electromagnetic material properties, such as relative permittivity and relative permeability, using the `electromagneticProperties` function.
- Specify a charge density and current density using the `electromagneticSource` function.
- Set electromagnetic boundary conditions, such as voltage and magnetic potential, using the `electromagneticBC` function.

The `solve` function solves electrostatic or magnetostatic problems and returns the values of electric or magnetic potential, field, and flux density at nodal locations of the mesh. You can analyze the resulting solution further by using one of these functions:

- `interpolateElectricPotential` and `interpolateMagneticPotential` interpolate the electric and magnetic potential at nodes to arbitrary spatial locations.
- `interpolateElectricField` and `interpolateMagneticField` interpolate the electric and magnetic field at nodes to arbitrary spatial locations.
- `interpolateElectricFlux` and `interpolateMagneticFlux` interpolate the electric and magnetic flux density at nodes to arbitrary spatial locations.

The `pdeplot` function visualizes the solution by plotting the resulting potentials, fields, fluxes, and mesh.

For more details about the new workflow, see Electromagnetics.

3-D Geometries: Create a multidomain geometry by inserting one geometry into another

Combine two 3-D geometries or create void regions inside 3-D geometry using the `addCell` and `addVoid` functions. For these operations, all cells of one geometry must be contained inside one cell of the other geometry.

Geometry Extrusion: Extrude faces of a 3-D geometry to a specified height

Extrude faces of a 3-D geometry along the direction normal to all specified faces using the `extrude` function. You can extrude faces into multiple layers by specifying a vector `height` of thicknesses of the layers. All faces must be flat and must have the same orientation.

Geometry Queries: Find faces, edges, and cells based on their proximity to other geometric entities

The following functions support geometry queries. They return face and edge IDs that you can use as arguments for other functions.

- `cellFaces` and `cellEdges` find faces and edges attached to the specified cells.
- `faceEdges` finds edges attached to the specified faces.
- `facesAttachedToEdges` finds faces attached to the specified edges.
- `nearestFace` and `nearestEdge` find faces and edges closest to the specified points.

Geometry Import from STL Files: Import a geometry without creating a model

The `importGeometry` function now lets you create a geometry object from an STL geometry file without attaching the imported geometry to any model. The new syntax is `g = importGeometry('geometryfile.stl')`. This approach lets you modify and adapt the geometry to meet your requirements before attaching it to a model. It also lets you share the same geometry between models.

PDEVisualization object: Create and plot an object containing nodal data, mesh, and visualization options as its properties

The `pdeviz` function uses the mesh and nodal data to create a `PDEVisualization` object and plot the result. You can interact with the resulting plot by changing the properties of this object. For example, you can change the mesh visibility, transparency, mesh deformation, axes labels, and so on. The plot reflects the new settings without the need to plot the same data repeatedly.

Face Addition and Geometry Transformation for Analytic Geometries: addFace, rotate, scale, and translate now work with AnalyticGeometry objects

The `addFace` function now lets you fill void regions in 2-D `AnalyticGeometry` objects.

The `rotate`, `scale`, and `translate` functions now work on `AnalyticGeometry` objects.

PDE Conversion to Divergence Form: Convert PDEs into the form required by Partial Differential Equation Toolbox using Symbolic Math Toolbox functions

Partial Differential Equation Toolbox solves equations of the form

$$\mathbf{m}\frac{\partial^2 \mathbf{u}}{\partial t^2} + \mathbf{d}\frac{\partial \mathbf{u}}{\partial t} - \nabla \cdot (\mathbf{c} \otimes \nabla \mathbf{u}) + \mathbf{a}\mathbf{u} = \mathbf{f}$$

The `pdeCoefficients` (Symbolic Math Toolbox) and `pdeCoefficientsToDouble` (Symbolic Math Toolbox) functions convert PDEs into this form and extract the coefficients into a structure that can

be used by the `specifyCoefficients` function. For example, see Solve Partial Differential Equation of Nonlinear Heat Transfer (Symbolic Math Toolbox).

R2020b

Version: 3.5

New Features

Bug Fixes

3-D Geometry Creation: Extrude a 2-D geometry into a 3-D geometry

Extrude a planar geometry along the *z*-axis to obtain a 3-D geometry. For details, see 3-D Multidomain Geometry from 2-D Geometry and `extrude`.

Finite Element Matrices for Custom Workflows: Assemble FE matrices for time-dependent and nonlinear models

The `assembleFEMatrices` function, which returns global finite element matrices for structural, thermal, and general PDE models can now:

- Assemble a subset of matrices, such as updated load only or stiffness only, to save computation time
- Assemble matrices using input time or solution for a time-dependent or nonlinear model, respectively

R2020a

Version: 3.4

New Features

Bug Fixes

Compatibility Considerations

Axisymmetric Analysis: Speed up simulations by simplifying 3-D solids of revolution by analyzing only the 2-D axisymmetric sections

Simplify 3-D structural and thermal problems to 2-D using their symmetry around the axis of rotation. The toolbox now supports an axisymmetric analysis for linear elasticity and heat transfer problems and enables you to:

- Create an axisymmetric 2-D model for a structural or thermal problem. See `createpde`.
- Set up an axisymmetric problem and analyze the results in cylindrical coordinates. In particular, you can specify the enforced displacement for a structural axisymmetric model. See `structuralBC`.
- Model the effect of a spinning axisymmetric structure by specifying a centrifugal load. For details, see `structuralBodyLoad`.

For a heat transfer example, see Heat Distribution in Circular Cylindrical Rod.

Multidomain Geometry: Split cells and fill voids to create multiple domains with different properties

Use the `addFace` function to create new geometric faces in 2-D and 3-D geometries. Adding a new face lets you modify a geometry:

- In a 2-D geometry, a new face fills a void region. The new face can have its own properties, such as thermal or structural material properties, or become an internal heat source.
- In a 3-D geometry, a new face splits a cell into two cells. Splitting cells lets you convert a single domain geometry (created by `importGeometry`, for example) to a multidomain geometry. Each cell (domain) can have its own properties.

Geometry Transformation: Manipulate geometries to preferred orientation and size by rotation, scaling, and translation

The toolbox supports these geometry transformations:

- Rotation around an arbitrary axis using the `rotate` function.
- Scaling up or down along each Cartesian axis independently with respect to a reference point using the `scale` function.
- Translation in any direction using the `translate` function.

Modal Damping: Include damping in modal transient and frequency response simulations

For modal transient and modal frequency response models, specify damping as a percentage of critical damping for a selected vibration frequency. The toolbox enables you to specify the modal damping parameter as:

- Constant modal damping ratio for all modes
- Frequency-dependent modal damping ratio using a function handle

See `structuralDamping` and Dynamics of Damped Cantilever Beam.

pdegplot, pdemesh, pdeplot, and pdeplot3D Functions: Improved performance for plots with many text labels

The PDE plotting functions show faster rendering and better responsiveness for plots that display many text labels. For example, this code shows about a 3x increase in speed:

```
model = createpde;
importGeometry(model,'Block.stl')
generateMesh(model)
pdemesh(model,'NodeLabels','on')
```

Compatibility Considerations

Code containing `findobj(fig,'Type','Text')` no longer returns labels on figures produced by the PDE plotting functions.

R2019b

Version: 3.3

New Features

Bug Fixes

Reduced Order Modeling: Approximate dynamic characteristics of a structural model for faster execution

The toolbox now supports the Craig-Bampton component mode synthesis workflow for structural mechanics.

Finite-element discretized models can be very large. Model order reduction techniques approximate the dynamics of the original system with a smaller system while retaining most of the dynamic characteristics.

When using the reduced-order model workflow, you can:

- Specify structural superelement interfaces. See `structuralSEInterface`.
- Reduce a structural analysis model to all modes in the specified frequency range and the interface degrees of freedom. See `reduce`.

Simscape Multibody Models: Generate dynamic substructure for flexible multibody simulations

You can use results obtained with the model order-reduction technique to provide data for Simscape™ Multibody™ flexible body block.

Simscape models expect the connections at all joints to have six degrees of freedom, while Partial Differential Equation Toolbox uses two or three degrees of freedom at each node. To interface with Simscape joints, set multipoint constraints by using the `structuralBC` function. Setting a multipoint constraint ensures that all nodes and all degrees of freedom have a rigid constraint with the geometric center of all specified geometric regions together as the reference point. The reference location has six degrees of freedom.

To recover a full-model transient solution from reduced-order model results and Simscape solution, use the `reconstructSolution` function.

For an example of a Simscape Multibody workflow that uses a reduced order model, see Model an Excavator Dipper Arm as a Flexible Body (Simscape Multibody).

Frequency Response Analysis: Determine dynamic response of a structure in the frequency domain

Determining the dynamic response of a structure under various forms of excitation is a common task in structural analysis. This problem can be formulated over time domain (in which case it is called transient response analysis) or frequency domain (called frequency response analysis or sometimes harmonic analysis).

In addition to the transient dynamic analysis, the toolbox now supports the frequency response analysis for structural models. When setting up a linear elasticity problem, you can:

- Create a special model container for a frequency response structural analysis. See `createpde`.
- Specify a boundary load, for example, pressure. See `structuralBoundaryLoad`.
- Solve the problem and obtain displacement, velocity, acceleration, and solution frequencies at nodal locations of the mesh. See `solve`.

- To speed up computations, you can use modal analysis results for frequency response analysis. The `ModalResults` argument triggers the `solve` function to use the modal superposition method.

Structural Analysis: Set concentrated boundary conditions at arbitrary locations on geometry surfaces

Use `addVertex` to create new vertices at any points on boundaries of a 2-D or 3-D geometry represented by a `DiscreteGeometry` object. Then use `structuralBC` or `structuralBoundaryLoad` to set concentrated boundary constraints and loads at these vertices.

For an example of applying a point load on a geometric boundary, see Reduced-Order Modeling Technique for Beam with Point Load.

Eigenvalue Solver Options: Specify parameters for Lanczos algorithm

Solvers for structural modal analysis problems and reduced-order modeling use the Lanczos algorithm. Use `PDESolverOptions` to specify the maximum number of Lanczos shifts and the block size for block Lanczos recurrence.

R2019a

Version: 3.2

New Features

Bug Fixes

Structural Analysis: Set boundary constraints and loads on edges and vertices

The workflow for structural analysis problems lets you specify an enforced displacement and the `'free'` and `'fixed'` boundary constraints on vertices and edges for both 2-D and 3-D models. To specify boundary constraints and a displacement, including spatial components of displacement, use the `structuralBC` function. The previous versions of this function let you specify the displacement and boundary constraints values only on edges for 2-D models and faces on 3-D models.

You can specify concentrated force at a vertex by using the `structuralBoundaryLoad` function.

Structural Analysis: Compute transient response by using the modal superposition method

By default, the `solve` function uses the direct integration approach which can be slow. To speed up calculations, transient dynamics analysis can be performed using modal analysis results. The new `ModalResults` argument triggers the `solve` function to switch to the modal transient solver instead of using the direct integration approach.

Finite Element Matrices: Assemble global finite element matrices for thermal and structural models

The `assembleFEMatrices` function accepts thermal and structural models with time- and solution-independent coefficients.

R2018b

Version: 3.1

New Features

Bug Fixes

Thermal Load: Evaluate thermal stress and thermal expansion in static structural analysis

The programmatic workflow for static structural analysis problems now lets you account for thermal loading. When setting up a static structural problem, you can:

- Specify a coefficient of thermal expansion as a structural material property. See `structuralProperties`.
- Specify a thermal load as a body load. Use a constant temperature to specify a steady and uniform thermal load or use previously obtained results of thermal analysis to specify a nonuniform thermal load. See `structuralBodyLoad`.
- Specify a reference temperature. This temperature corresponds to the state of the model at which both thermal stress and strain are zeros. See `StructuralModel`.

The `solve` function solves a static structural analysis model accounting for mechanical and thermal effects. The function returns a displacement, stress, strain, and von Mises stress induced by both mechanical and thermal loads.

For an example of the new workflow, see Thermal Deflection of Bimetallic Beam.

R2018a

Version: 3.0

New Features

Bug Fixes

Compatibility Considerations

Structural Analysis: Solve linear transient dynamic problems using direct time integration

The programmatic workflow for structural analysis problems now lets you set up, solve, and analyze dynamic linear elasticity problems using a familiar domain-specific language. Most steps correspond to the similar steps for setting up a static linear elasticity problem. Additional options for a dynamic linear elasticity problem include:

- Specifying proportional (Rayleigh) mass and stiffness damping parameters. See `structuralDamping`.
- Specifying initial conditions. See `structuralIC`.
- Specifying time-dependent boundary loads by using function handles. Also, you can specify the form and duration of the pressure pulse and the frequency and phase of sinusoidal pressure by using the corresponding name-value pair arguments. See `structuralBoundaryLoad`.
- Specifying time-dependent boundary loads by using function handles. Also, you can specify the form and duration of x-, y-, or z-component of the enforced displacement and the frequency and phase of sinusoidal displacement by using the corresponding name-value pair arguments. See `structuralBC`.

The `solve` function solves a dynamic structural analysis model and returns displacement, velocity, and acceleration at nodal locations of the mesh. You can analyze the resulting solution further by using one of these functions:

- `evaluateStress` evaluates stress at nodal locations for all time steps.
- `evaluateStrain` evaluates strain at nodal locations for all time steps.
- `evaluateVonMisesStress` evaluates von Mises stress at nodal locations for all time steps.
- `evaluateReaction` evaluates reaction forces on a specified boundary.
- `evaluatePrincipalStress` and `evaluatePrincipalStrain` evaluate principal stress and strain at mesh nodes.
- `interpolateDisplacement` interpolates displacements at arbitrary spatial locations.
- `interpolateVelocity` interpolates velocities at arbitrary spatial locations.
- `interpolateAcceleration` interpolates accelerations at arbitrary spatial locations.
- `interpolateStress` and `interpolateStrain` interpolate stress and strain at arbitrary spatial locations.
- `interpolateVonMisesStress` interpolates von Mises stress at arbitrary spatial locations.

For more details about the new workflow, see Structural Mechanics.

Modal Analysis: Find natural frequencies and mode shapes

The programmatic workflow for modal analysis problems lets you find natural frequencies and mode shapes of a structure. Use the same steps for creating a modal analysis model and specifying materials and boundary constraints as for static linear elasticity problems. When solving a modal analysis model, the solver requires a frequency range parameter and returns the modal solution in that frequency range. See Vibration of Square Plate.

Mesh Analysis: Assess element quality, measure element area or volume, and find nodes and elements

The `findElements` and `findNodes` functions return collections of mesh elements and nodes associated with a particular geometric region (edge, face, and so on), located within a bounding box or disk, or located close to a specified point or node. These functions return node or element IDs that you can use as arguments for other mesh query functions or plotting functions.

The `meshQuality` function lets you assess shape quality of mesh elements of an entire mesh or a particular group of elements. Using this function, you can analyze the shape quality of each element of a 2-D or 3-D mesh, locate the elements of low quality, and adjust you mesh-generation parameters accordingly.

The `area` and `volume` functions measure areas and volumes covered by individual elements and groups of elements of 2-D and 3-D meshes, respectively.

The `pdemesh`, `pdeplot`, and `pdeplot3D` functions accept node and element IDs as input arguments, which lets you highlight particular nodes and elements on mesh plots.

Geometry from Mesh: Create multidomain geometry from nodes and elements

The `geometryFromMesh` function creates a geometric model from a triangulated mesh, including planar, volume, and surface triangulation that bounds a closed volume. This function lets you create a multidomain geometry by specifying the subdomain ID for each element of the mesh. You can retain the original mesh or generate a new one by using the `generateMesh` function.

Functionality Being Removed or Changed

Functionality	Result	Use Instead	Compatibility Considerations
pdesdp	Still runs	findNodes	Use a `PDEModel` object to set up and solve a PDE problem. For the step-by-step workflow, see Solve Problems Using PDEModel Objects. `PDEModel` stores a finite element mesh as a `FEMesh` object in its `Mesh` property. Use the `findNodes` function to find mesh nodes that belong to particular regions.
pdesdt	Still runs	findElements	Use `findElements` to find mesh elements that belong to particular regions.
pdetrg	Still runs	area	Use the `area` function to compute areas of 2-D mesh elements.
pdetriq	Still runs	meshQuality	Use the `meshQuality` function to evaluate shape quality of mesh elements.

Functionality	Result	Use Instead	Compatibility Considerations
pdegrad	Still runs	evaluateGradient	Use the evaluateGradient function to evaluate the gradient of a PDE solution.
pdecgrad	Still runs	evaluateCGradient	Use the evaluateCGradient function to evaluate the flux of a PDE solution.

R2017b

Version: 2.5

New Features

Bug Fixes

Compatibility Considerations

Structural Analysis: Solve static linear elasticity problems

A new programmatic workflow lets you set up, solve, and analyze static linear elasticity problems using a familiar domain-specific language. When setting up a static linear elasticity problem, you can:

- Create a special model container for a static structural analysis. See `createpde`.
- Assign structural properties of the material, such as Young's modulus, Poisson's ratio, and mass density. See `structuralProperties`.
- Specify a body load for a structural model. See `structuralBodyLoad`.
- Specify pressure, surface traction, and translational stiffness for a particular boundary. See `structuralBoundaryLoad`.
- Specify enforced displacement and boundary constraints for a particular boundary. See `structuralBC`.

The `solve` function solves a static structural analysis model and returns displacement, stress, strain, and von Mises stress at nodal locations of the mesh. You can analyze the resulting solution further by using one of these functions:

- `interpolateDisplacement` interpolates displacements at arbitrary spatial locations.
- `interpolateStress` and `interpolateStrain` interpolate stress and strain at arbitrary spatial locations.
- `interpolateVonMisesStress` interpolates von Mises stress at arbitrary spatial locations.
- `evaluateReaction` evaluates reaction forces on a specified boundary.
- `evaluatePrincipalStress` and `evaluatePrincipalStrain` evaluate principal stress and strain at mesh nodes.

The `pdeplot` and `pdeplot3D` functions let you visualize the solution by plotting the resulting displacements, stresses, and strains.

For more details about the new workflow, see Structural Mechanics.

Planar STL Geometry: Import and mesh planar STL geometries

`importGeometry` can import a planar STL geometry and convert it to a 2-D geometry by mapping it to the X-Y plane. To mesh the resulting 2-D geometry, use `generateMesh`.

Meshing: Improved mesh generation

The mesh generator, `generateMesh`, now:

- Uses new mesh generation algorithm for 2-D geometries.
- Lets you specify mesh growth rate for both 2-D and 3-D meshes. To specify mesh growth rate, use the `Hgrad` argument of `generateMesh`.

Compatibility Considerations

Resulting meshes can differ from meshes generated in previous releases. For example, meshes generated with the default size controls can have fewer elements than before.

Also, `generateMesh` creates quadratic meshes for 2-D problems by default. In previous releases, the default mesh for 2-D geometries is a linear mesh. For both 2-D and 3-D geometries, you can specify whether you want to use linear or quadratic mesh by using the `GeometricOrder` argument of `generateMesh`.

Functionality Being Removed or Changed

Functionality	Result	Use Instead	Compatibility Considerations
Function handle for specifying nonconstant boundary conditions and coefficients of the form `@f(problem, region,state)`	Still runs	`@f(region,state)`	Use the two-argument form, `@f(region,state)`, to define a function handle for `applyBoundaryCondition` or `specifyCoefficients`.
pdetool	Still runs	pdeModeler	The function name `pdetool` has been changed to `pdeModeler`.
Opening the PDE Modeler app by calling `pdeModeler` or `pdetool` or by using the **Apps** tab	Does not overwrite existing information in the app anymore	To overwrite the existing information in the PDE Modeler app, select **File > New**.	In previous releases, starting the PDE Modeler app and then reopening the app by calling `pdetool` or by using the **Apps** tab overwrites any existing information in the app. Now, reopening the PDE Modeler app brings focus to the app window.
`Jiggle`, `JiggleIter`, and `MesherVersion` arguments of `generateMesh`	Ignored	No replacement	`generateMesh` produces good quality meshes without jiggling the nodes.

R2017a

Version: 2.4

New Features

Bug Fixes

Compatibility Considerations

Thermal Analysis: Solve conduction-dominant heat transfer problems with convection and radiation occurring at boundaries

A new programmatic workflow lets you set up, solve, and analyze conduction-dominant heat transfer problems using natural steps and familiar domain-specific language. When setting up a heat transfer problem, you can:

- Create a special model container for a steady-state or transient thermal model. See `createpde`.
- Assign thermal properties of the material, such as thermal conductivity, specific heat, and mass density. See `thermalProperties`.
- Specify internal heat sources of the geometry. See `internalHeatSource`.
- Set temperatures on boundaries, specify insulated boundaries, heat fluxes through boundaries, convection coefficients, radiation emissivity coefficients, and ambient temperature. See `thermalBC`.
- Set initial temperature or initial guess for temperature. See `thermalIC`.

The `solve` function solves steady-state and transient thermal models and returns temperatures and temperature gradients at nodal locations of the thermal model mesh. You can analyze the resulting solution further by using one of these functions:

- `interpolateTemperature` interpolates resulting temperatures to arbitrary spatial locations.
- `evaluateTemperatureGradient` evaluates temperature gradient for a transient thermal solution at arbitrary spatial locations.
- `evaluateHeatFlux` evaluates heat flux of a thermal solution at nodal or arbitrary spatial locations.
- `evaluateHeatRate` evaluates integrated heat flow rate normal to specified boundary.

The `pdeplot` and `pdeplot3D` functions let you visualize a thermal model solution by plotting the resulting temperatures, and temperature gradients, and mesh.

There is a new featured example showing heat transfer in a transient 3-D model, Heat Conduction in a Spherical Multidomain Geometry with Nonuniform Heat Flux.

For more details about the new workflow, see Heat Transfer.

3-D Multidomain Geometry: Create geometries consisting of stacked or nested cuboids, spheres, or cylinders

The `multicuboid`, `multicylinder`, and `multisphere` functions create 3-D geometries formed by several cubic, cylindrical, and spherical cells, respectively. With these functions, you can create stacked or nested geometries. You also can create geometries where some cells are empty, for example, hollow cylinders, cubes, or spheres.

All cells in a geometry must be of the same type: either cuboids, or cylinders, or spheres. These functions do not combine cells of different types in one geometry.

Functionality Being Removed or Changed

Functionality	Result	Use Instead	Compatibility Considerations
`pdemdlcv`	Errors	No replacement	Remove all instances of `pdemdlcv`.
Function handle for specifying nonconstant boundary conditions and coefficients of the form`@f(problem, region,state)`.	Still runs	`@f(region,state)`	Use the two-argument form, `@f(region,state)`, to define a function handle for `applyBoundaryCondition` or `specifyCoefficients`.

R2016b

Version: 2.3

New Features

Bug Fixes

Compatibility Considerations

Flux of PDE Solution: Evaluate tensor product of c-coefficient and gradient of PDE solution for 2-D and 3-D problems

The `evaluateCGradient` function computes the tensor product of c-coefficient and gradients of the PDE solution, $\mathbf{c} \otimes \nabla \mathbf{u}$, at nodal or arbitrary locations in 2-D or 3-D geometry.

Boundary Conditions: Set an individual boundary condition for each equation in a PDE system, query boundary condition assignments

The `applyBoundaryCondition` function can set an individual boundary condition for each equation in a system of PDEs in one function call. For example, in a system of two PDEs, one `applyBoundaryConditions` call can set the Dirichlet boundary condition for the first equation, and the Neumann boundary condition for the second equation.

The function uses clear precedence rules to decide which condition to use for every geometric region.

The `findBoundaryConditions` function returns the currently used boundary condition assignment for a geometric region.

Compatibility Considerations

The new syntax requires explicit specification of the boundary condition type as `'dirichlet'`, `'neumann'`, or `'mixed'`. For example, in previous releases you used the following syntaxes to apply the Dirichlet boundary condition on edge 1 and Neumann boundary condition on face 2.

```
applyBoundaryCondition(model,'Edge',1,'u',0);
applyBoundaryCondition(model,'Face',2,'g',0,'q',0);
```

Update them to specify the boundary condition types.

```
applyBoundaryCondition(model,'dirichlet','Edge',1,'u',0);
applyBoundaryCondition(model,'neumann','Face',2,'g',0,'q',0);
```

Previously, to set the Dirichlet boundary condition for one equation in a PDE system and the Neumann boundary condition for another, you used two function calls to `applyBoundaryCondition`.

```
applyBoundaryCondition(model,'edge',4,'u',0,'EquationIndex',1);
applyBoundaryCondition(model,'edge',4,'g',[0,-1]);
```

Now, set both boundary conditions in one function call by specifying the boundary condition type as `'mixed'`.

```
applyBoundaryCondition(model,'mixed','edge',4,'u',0,...
                       'EquationIndex',1,'g',[0,-1]);
```

Nodal Initial Conditions: Set nodal initial conditions using the result of a previous simulation

The `setInitialConditions` function sets initial conditions at the mesh nodes by using the solution from a previous analysis on the same geometry and mesh.

Geometric Initial Conditions: Set initial conditions on vertices, edges, faces, and cells

The `setInitialConditions` function sets initial conditions on faces, edges, and vertices for both 2-D and 3-D geometries, and on cells for 3-D geometry. You can set initial conditions on particular vertices, edges, faces, and cells or set global initial conditions on all vertices, edges, faces, or cells in the geometry.

Mesh and Solution Plots: Set transparency, display node and element labels

The `FaceAlpha` argument of `pdegplot`, `pdemesh`, `pdeplot`, and `pdeplot3D` lets you set the plot transparency.

The `ElementLabels` argument of `pdemesh`, `pdeplot`, and `pdeplot3D` lets you display element labels.

The `NodeLabels` argument of `pdemesh` and `pdeplot` lets you display node labels.

The `VertexLabels` and `CellLabels` arguments of `pdegplot` let you display vertex and cell labels.

Compatibility Considerations

The argument `SubdomainLabels` is no longer recommended. Use `FaceLabels` for 2-D geometries instead.

3-D Geometry Import from STL Files: Improved quality of the resulting geometry

When importing an STL geometry for a 3-D problem, `importGeometry` can recognize and reconstruct more geometric vertices, edges, and faces of the original CAD geometry in some instances. In these cases, the resulting geometry is a closer match to the original CAD geometry.

Compatibility Considerations

Detailed geometries can now contain more faces and edges than in previous releases. As a result, in rare instances, the new faces and edges can cause renumbering of the existing ones. If your code imports an STL geometry, visually check the geometry to ensure that you are assigning boundary and initial conditions to the intended regions.

Functionality Being Removed or Changed

Functionality	Result	Use Instead	Compatibility Considerations
pdemdlcv	Warns	No replacement	Remove all instances of pdemdlcv.

Functionality	Result	Use Instead	Compatibility Considerations
pde	Errors	createpde	Use createpde to create a PDEModel that holds the PDE analysis data. The pde class was a value class. The replacement PDEModel class is a handle class.
pdeGeometryFromEdges	Errors	geometryFromEdges	Use geometryFromEdges instead. Although pdeBoundaryConditions still runs with a warning, its returned type has changed from a pdeGeometry object to an AnalyticGeometry object. The pdeGeometry class was a value class. The replacement AnalyticGeometry class is a handle class.
pdeBoundaryConditions	Errors	applyBoundaryCondition	Replace all instances of pdeBoundaryConditions(ApplicationRegion,...) with applyBoundaryCondition(model,BCType,'edge',EdgeID,...) Although pdeBoundaryConditions still runs with a warning, its returned type has changed from a pdeBoundaryConditions object to a 1BoundaryCondition object. The pdeBoundaryConditions class was a value class. The replacement BoundaryCondition class is a handle class.
Function handle for specifying nonconstant boundary conditions and coefficients of the form @f(problem, region,state).	Still runs	@f(region,state)	Use specifyCoefficients and define a function handle that takes only two arguments: @f(region,state)

R2016a

Version: 2.2

New Features

Bug Fixes

Compatibility Considerations

PDE Solvers: Use solvepde and solvepdeeig functions to solve PDEs and PDE eigenvalue problems

New solver functions for `PDEModel`:

- `solvepde` replaces `assempde`, `pdenonlin`, `hyperbolic`, and `parabolic`.
- `solvepdeeig` replaces `pdeeig`.

To use the new solvers, include PDE coefficients in your model using `specifyCoefficients`. Include initial conditions in your model using `setInitialConditions`.

The new solvers return results as one of the three new objects:

- `StationaryResults` — Returned by `solvepde` for a stationary PDE model.
- `TimeDependentResults` — Returned by `solvepde` for a time-dependent PDE model.
- `EigenResults` — Returned by `solvepdeeig`.

`StationaryResults` and `TimeDependentResults` objects contain solution gradients at the nodes.

PDE Coefficients: Specify equation coefficients as a property of PDEModel

The `specifyCoefficients` function specifies equation coefficients as a property of `PDEModel`.

Initial Conditions: Set initial conditions or initial guess as a property of PDEModel

The `setInitialConditions` function specifies initial conditions as a property of `PDEModel`.

Quadratic Elements for 2-D Mesh: Generate 2-D mesh using quadratic triangular elements

Create a quadratic mesh for 2-D problems using `generateMesh` with `GeometricOrder` set to `'quadratic'`.

Gradient of PDE Solution: Evaluate solution gradient at arbitrary 2-D or 3-D points

The `evaluateGradient` function enables you to interpolate the gradient of a `StationaryResults` or `TimeDependentResults` object at arbitrary points in the geometry.

Finite Element Matrices: Use assembleFEMatrices to assemble finite element matrices

The `assembleFEMatrices` function assembles finite element matrices for independent factoring and solution using linear algebra methods. It replaces `assempde`, `assema`, and `assemb` for matrix assembly.

PDE Results for Plotting and Postprocessing: New result objects depend on the type of PDE

The `createPDEResults` function returns results as one of the three new objects, depending on the type of the PDE problem.

- A `StationaryResults` object for a stationary PDE model. `StationaryResults` contains the solution of PDE and its gradients at the nodal locations.
- A `TimeDependentResults` object for a time-dependent PDE model. `TimeDependentResults` contains the solution of PDE and its gradients at the nodal locations.
- A `EigenResults` object for an eigenvalue problem.

Compatibility Considerations

`createPDEResults` no longer creates an object of type `PDEResults`.

The syntax of `createPDEResults` has changed to accommodate creating the new result types for time-dependent and eigenvalue problems.

- To create the `TimeDependentResults` object for a time-dependent problem, use the syntax `createPDEResults(pdem,u,utimes,'time-dependent')`, where `utimes` is a vector of solution times.
- To create the `EigenResults` object for an eigenvalue problem, use the syntax `createPDEResults(pdem,eigenvectors,eigenvalues,'eigen')`.

`EigenResults` has different property names than `PDEResults`. Update any eigenvalue scripts that use `PDEResults` property names.

Functionality Being Removed or Changed

Functionality	Result	Use Instead	Compatibility Considerations
wbound	Still runs	No replacement	New features and the recommended workflow are not compatible with this function. For the recommended workflow, see Solve Problems Using PDEModel Objects.
pdeadgsc and pdeadworst	Still runs	No replacement	New features and the recommended workflow are not compatible with these functions. For the recommended workflow, see Solve Problems Using PDEModel Objects.

Functionality	Result	Use Instead	Compatibility Considerations
`assempde`, `assema`, `assemb`, `hyperbolic`, `parabolic`, `pdenonlin`	Still runs	`solvepde` and `assembleFEMatrices`	To solve PDE problems, use `solvepde`. To obtain finite element matrices, use `assembleFEMatrices`. For the recommended workflow, see Solve Problems Using PDEModel Objects.
`pdeeig` and `sptarn`	Still runs	`solvepdeeig`	To solve PDE eigenvalue problems, use `solvepdeeig`. For the recommended workflow, see Solve Problems Using PDEModel Objects.
`poimesh`, `poiasma`, `poicalc`, `poiindex`, `poisolv`	Still runs	`solvepde`	To solve Poisson's equations, use `solvepde`. For details, see Solve Problems Using PDEModel Objects.
`pdejmps`	Still runs	No replacement	New features and the recommended workflow are not compatible with this function. For the recommended workflow, see Solve Problems Using PDEModel Objects.
`pdesmech`	Still runs	PDE app	Use the PDE app instead of `pdesmech`.
`dst` and `idst`	Still runs	No replacement	Remove all instances of `dst` and `idst`.
`tri2grid` and `pdeintrp`	Still runs	`interpolateSolution`	Use the interpolation function `interpolateSolution` provided by `StationaryResults`, `TimeDependentResults` and `EigenResults`.
`pdeprtni`	Still runs	No replacement	`NodalSolution` is a property of `StationaryResults` and `TimeDependentResults`. `Eigenvectors` is the corresponding property of `EigenResults`.
`pdemdlcv`	Still runs	No replacement	Remove all instances of `pdemdlcv`.
`pde`	Warns	`createpde`	Use `createpde` to create a `PDEModel` that holds the PDE analysis data. The `pde` class was a value class. The replacement `PDEModel` class is a handle class.

Functionality	Result	Use Instead	Compatibility Considerations
`pdeGeometryFromEdges`	Warns	`geometryFromEdges`	Use `geometryFromEdges` instead. Although `pdeBoundaryConditions` still runs with a warning, its returned type has changed from a `pdeGeometry` object to an `AnalyticGeometry` object. The `pdeGeometry` class was a value class. The replacement `AnalyticGeometry` class is a handle class.
`pdeBoundaryConditions`	Warns	`applyBoundaryCondition`	Replace all instances of `pdeBoundaryConditions(ApplicationRegion,...)` with `applyBoundaryCondition(model,'edge',EdgeID,...)` Although `pdeBoundaryConditions` still runs with a warning, its returned type has changed from a `pdeBoundaryConditions` object to a `BoundaryCondition` object. The `pdeBoundaryConditions` class was a value class. The replacement `BoundaryCondition` class is a handle class.
Loading a `pdeBoundaryConditions` object from an R2014b MAT file.	Errors	`applyBoundaryCondition`	Recreate the Boundary Conditions using `applyBoundaryCondition`.
Function handle for specifying nonconstant boundary conditions and coefficients of the form `@f(problem, region,state)`.	Still runs	`@f(region,state)`	Use `specifyCoefficients` and define a function handle that takes only two arguments: `@f(region,state)`

R2015b

Version: 2.1

New Features

Bug Fixes

Compatibility Considerations

3-D geometry creation from a finite element mesh using the geometryFromMesh function

The `geometryFromMesh` function creates 3-D geometry from a finite element mesh, or from a triangulated surface mesh. For details, see the function reference page or Create and View 3-D Geometry.

Data structure to represent solutions using the createPDEResults function

The `createPDEResults` function converts a PDE solution into a `PDEResults` object. The `PDEResults` object allows you to interpolate the solution using `interpolateSolution`. For details, see the reference pages.

Functionality Being Removed or Changed

Functionality	Result	Use Instead	Compatibility Considerations
pdesmech	Still runs	PDE app	Use the PDE app instead of pdesmech

R2015a

Version: 2.0

New Features

Bug Fixes

Compatibility Considerations

3-D finite element analysis

You can now solve partial differential equations with 3-D geometry. To do so, there is a new workflow that combines the geometry, mesh, and boundary conditions into a `PDEModel` object. You can also use this workflow for 2-D geometry. For details, see Solve Problems Using PDEModel Objects.

Equation coefficients and boundary conditions for 3-D problems

To specify problem coefficients or boundary conditions in 3-D geometry, you can use strings with a syntax similar to that of a 2-D problem. There is a new way of writing functions for coefficients in 3-D geometries. For details, see PDE Coefficients and Boundary Conditions.

Compatibility Considerations

To accommodate both 2-D and 3-D geometry, the format of boundary condition objects changed from that introduced in R2014b. The new object is BoundaryCondition Properties, and calling `pdeBoundaryConditions` now warns that it will be removed in a future release. If you saved a `pdeBoundaryConditions` object in an R2014b-format MAT file, then loading that file in R2015a can produce an error. Additionally, the syntax for specifying nonconstant boundary conditions has changed. Functions written in the previous syntax continue to work for now.

R2014b Syntax	R2015a Syntax
`function bcMatrix =` `myfun(problem,region,state)`	`function bcMatrix =` `myfun(region,state)`

For details, see Changes to Boundary Conditions Object From R2014b.

Elliptic, parabolic, hyperbolic, nonlinear, eigenvalue solvers for 3-D problems

The main toolbox solvers now support problems with 3-D geometry. For a listing of functions that do or do not support 3-D geometry, see Functions That Support 3-D Geometry. Solvers take a `model` argument instead of the previous `b`, `p`, `e`, `t` arguments. For details, see the function reference pages.

3-D geometry import from STL files

Import the geometry for a 3-D problem in the STL file format using the `importGeometry` function. For details, see Create and View 3-D Geometry.

3-D unstructured meshing using tetrahedra

Create finite element meshes using the `generateMesh` function. For 3-D geometry, the meshes consist of tetrahedra. See Mesh Data for [p,e,t] Triples: 3-D.

Plot function to inspect 3-D solutions

The `pdeplot3D` function plots solutions on the boundaries of 3-D geometry. For details, see Plot 3-D Solutions.

Featured examples with 3-D geometry

There are two new featured examples related to linear elasticity that have 3-D geometry:

- Deflection Analysis of a Bracket
- Vibration of a Square Plate

There is also a new example of plotting slices through a 3-D solution: Contour Slices Through a 3-D Solution.

To run the examples at the MATLAB® command line:

```
echodemo StrainedBracketExample
echodemo Eigenvaluesofa3DPlateExample
echodemo ContourSlices3DExample
```

pdebound and pdegeom reference pages removed

The pdebound and pdegeom reference pages have been replaced by the Boundary Conditions and 2-D Geometry documentation categories.

R2014b

Version: 1.5

New Features

Bug Fixes

Functions for modular definition of boundary conditions

To specify PDE boundary conditions in a modular fashion, per edge or set of edges, use a `pdeBoundaryConditions` specification. For details, see Steps to Specify a Boundary Conditions Object.

pdeInterpolant object for solution interpolation

Interpolate a PDE solution to a set of points using `evaluate` on an interpolant. Create the interpolant using `pdeInterpolant`.

R2014a

Version: 1.4

New Features

Bug Fixes

Damping option for hyperbolic solver

You can include damping in the `hyperbolic` solver in matrix form. There is a new example of dynamics of a damped cantilever beam that shows how to use this feature.

R2013b

Version: 1.3

New Features

Bug Fixes

Display option in hyperbolic and parabolic solvers

You can disable the display of internal ODE solution details that the `hyperbolic` and `parabolic` solvers report. To disable the display, set the `Stats` name-value pair to `'off'`.

Eigenvalue example

There is a new example of eigenvalues of a circular membrane. View the example here. To run the example at the MATLAB command line:

```
echodemo eigsExample
```

R2013a

Version: 1.2

New Features

Bug Fixes

Performance and robustness enhancements in meshing algorithm

The meshing (geometry triangulation) functions in `initmesh` and `adaptmesh` provide an enhancement option for increased meshing speed and robustness. Choose the enhanced algorithm by setting the `MesherVersion` name-value pair to `'R2013a'`. The default `MesherVersion` value of `'preR2013a'` gives the same mesh as previous toolbox versions.

The enhancement is available in `pdetool` from the **Mesh > Parameters > Mesher version** menu.

New example

There is a new example of heat distribution in a radioactive rod. View the example here. To run the example at the MATLAB command line:

```
echodemo radioactiveRod
```

R2012b

Version: 1.1

New Features

Compatibility Considerations

Coefficients of parabolic and hyperbolic PDEs that can be functions of the solution and its gradient

You can now solve parabolic and hyperbolic equations whose coefficients depend on the solution *u* or on the gradient of *u*. Use the `parabolic` or `hyperbolic` commands, or solve the equations using `pdetool`. For details, see the function reference pages.

Graphics export from pdetool

You can save the current `pdetool` figure in a variety of image formats. Save the figure using the **File > Export Image** menu. See File Menu.

pdegplot labels edges and subdomains

`pdegplot` now optionally labels:

*   The edges in the geometry
*   The subdomains in the geometry

To obtain these labels, set the `edgeLabels` or `subdomainLabels` name-value pairs to `'on'`. For details, see the `pdegplot` reference page.

New examples

There is a new example of uniform pressure load on a thin plate. View the example here. To run the example at the MATLAB command line:

```
echodemo clampedSquarePlateExample
```

There is a new example of nonlinear heat transfer in a thin plate. View the example here. To run the example at the MATLAB command line:

```
echodemo heatTransferThinPlateExample
```

There is a new example of a system of coupled PDEs. View the example here. To run the example at the MATLAB command line:

```
echodemo deflectionPiezoelectricActuator
```

pdesmech shear strain calculation change

The `pdesmech` function now calculates shear strain according to the engineering shear strain definition. This has always been the documented behavior. However, the previous calculation was performed according to the tensor shear strain calculation, which gives half the value of the engineering shear strain.

Compatibility Considerations

`pdesmech` now returns shear strain values exactly twice as large as before.